

# Characteristics of seismic wavefields in fluid-saturated fractured rocks

University of Lausanne, Switzerland

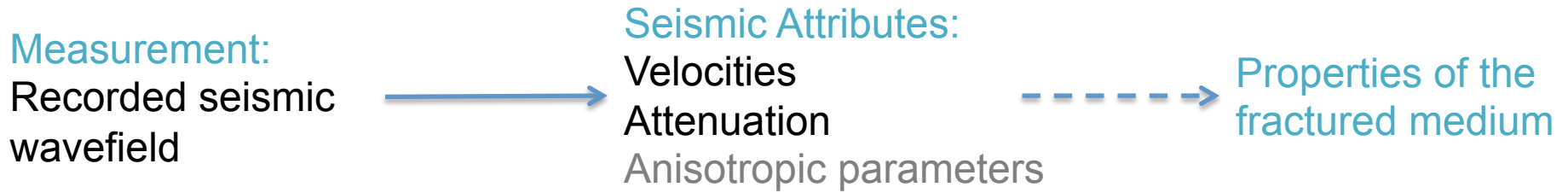
Università della Svizzera Italiana, Switzerland

Institute of Petroleum Geology and Geophysics SB RAS , Novosibirsk, Russia

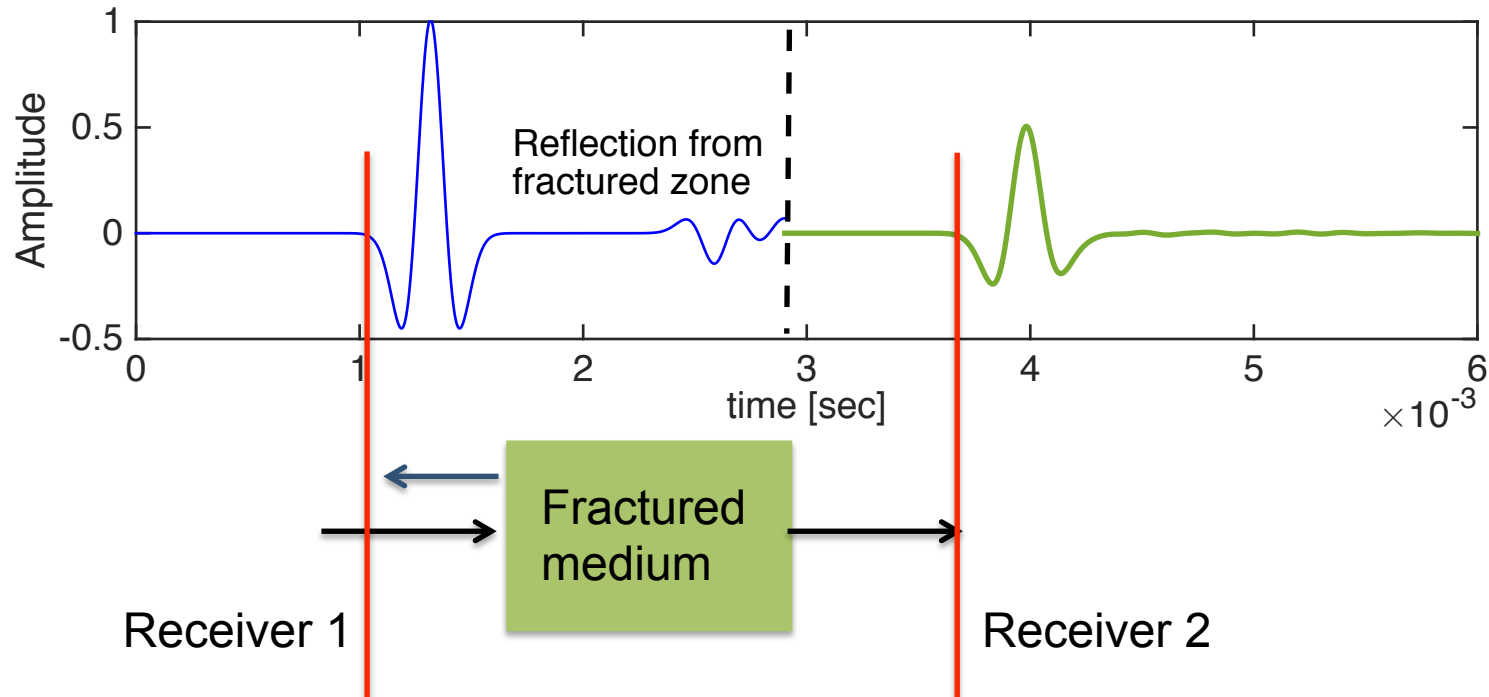
CONICET, Centro Atómico Bariloche – CNEA, Argentina

# Motivation

## Characteristics of fractured media from seismic wavefields



Physical Mechanisms?



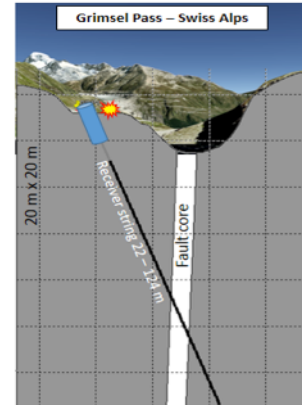
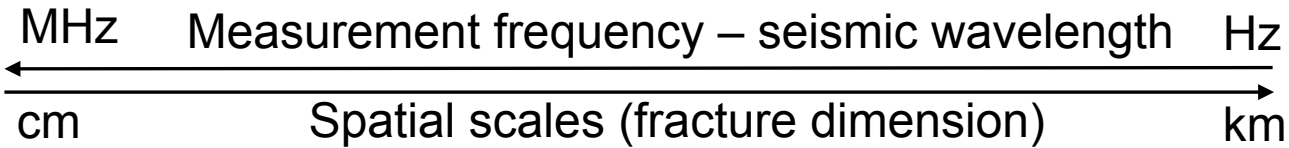
# Scales



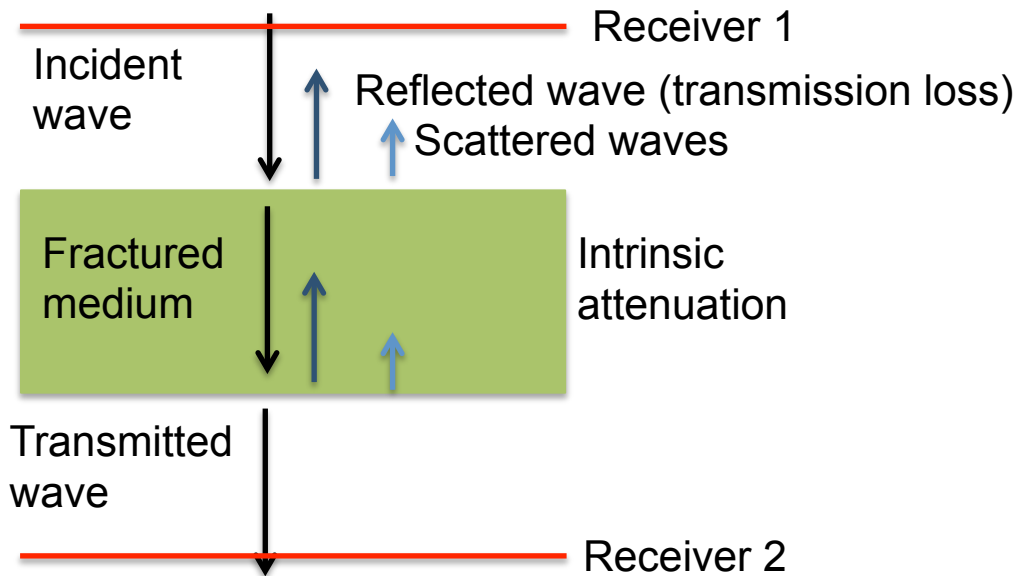
Laboratory data

Log data

Seismic data (VSP)



“Despite these striking scale differences the physical mechanisms are similar “



Attenuation

$$Q_p^{-1}(\omega) =$$

$$Q_{transmission}^{-1}(\omega)$$

$$+ Q_{scattering}^{-1}(\omega)$$

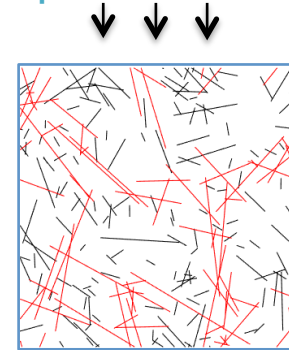
$$+ Q_{intrinsic}^{-1}(\omega)$$

# Outline

## Can we link intrinsic attenuation to fracture network properties?

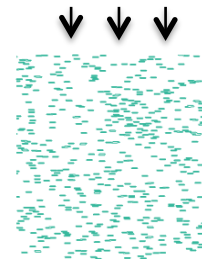
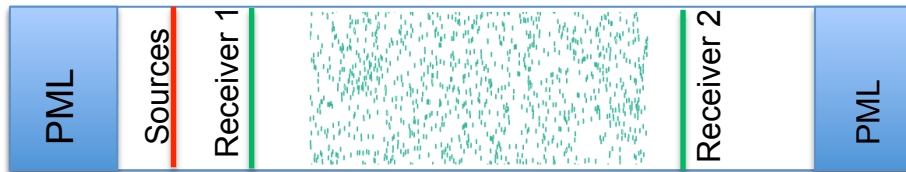
Numerical upscaling approach applied to stochastic fracture networks

- Wave propagation effects are ignored

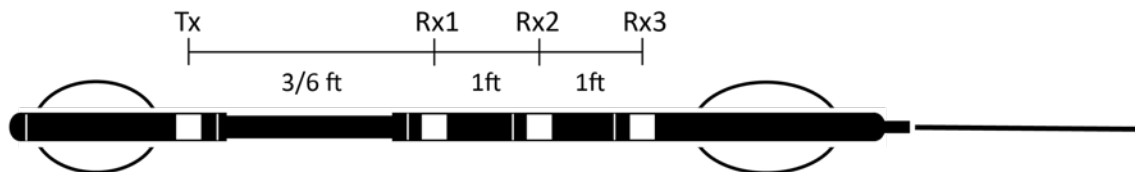


## The role played by wave propagation effects

A comparison of wave propagation modelling and numerical upscaling for simple models



## Application to full wave-form sonic data

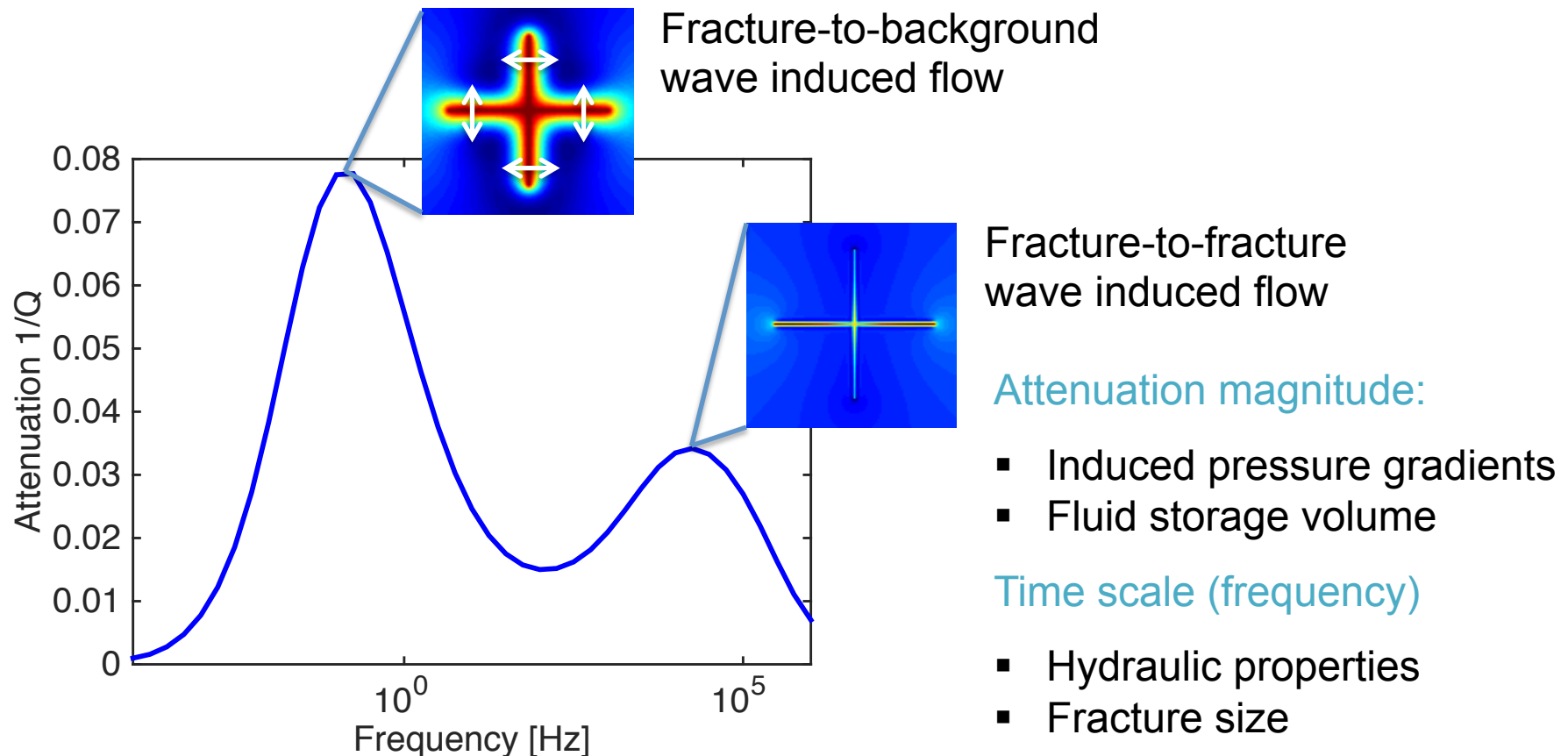


# Intrinsic attenuation – in fractured fluid saturated media

**Background:** stiff porous matrix of low porosity and permeability

**Fractures:** compliant inclusion of high porosity and permeability

**Mechanism:** Pressure diffusion processes (fractures  $\ll$  seismic wavelength)

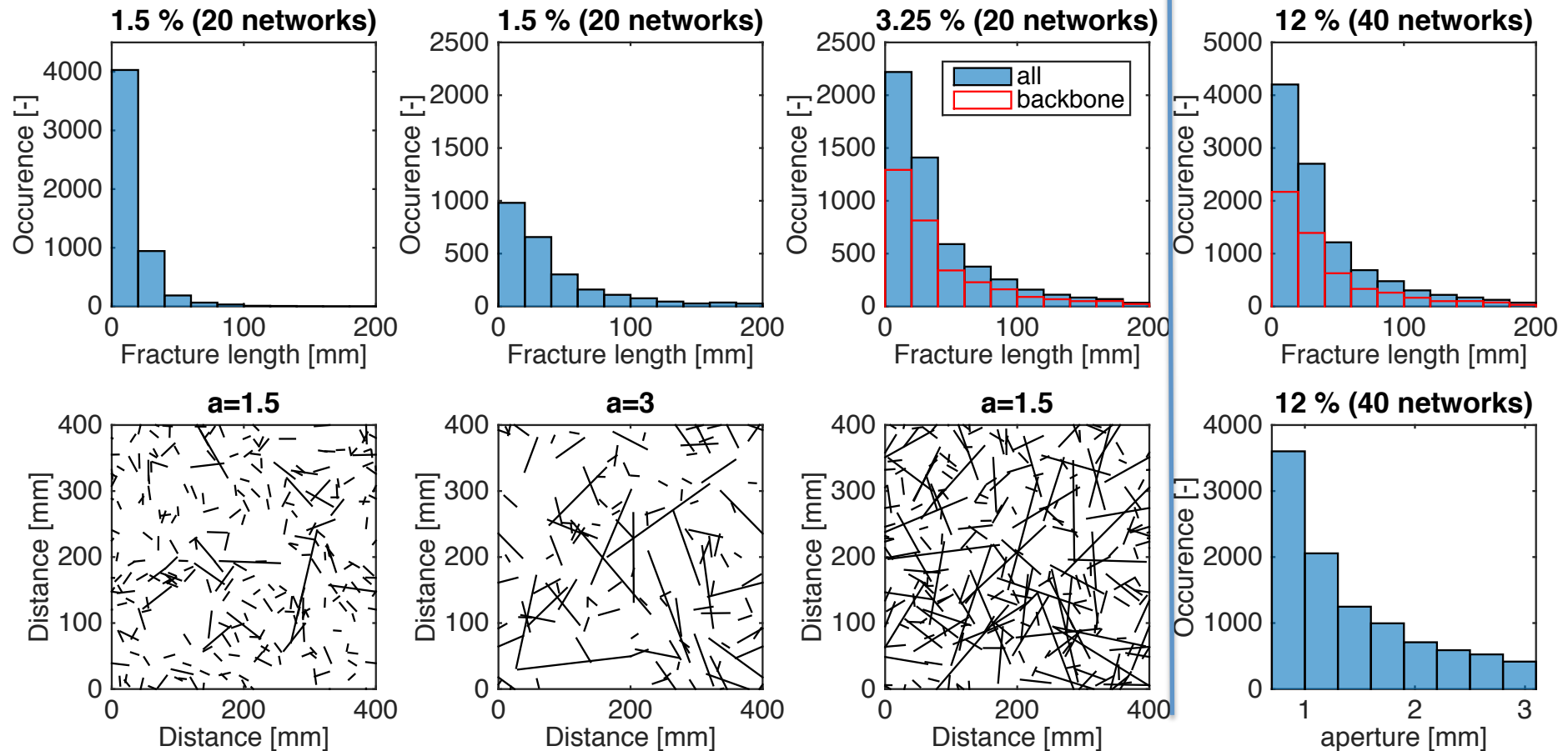


# Stochastic fracture networks

Fracture network parameter: 
$$n(l, L) = d_{frac} (a - 1) \frac{l^{-a}}{l_{min}^{-a+1}} \text{ for } l \in [l_{min}, l_{max}]$$

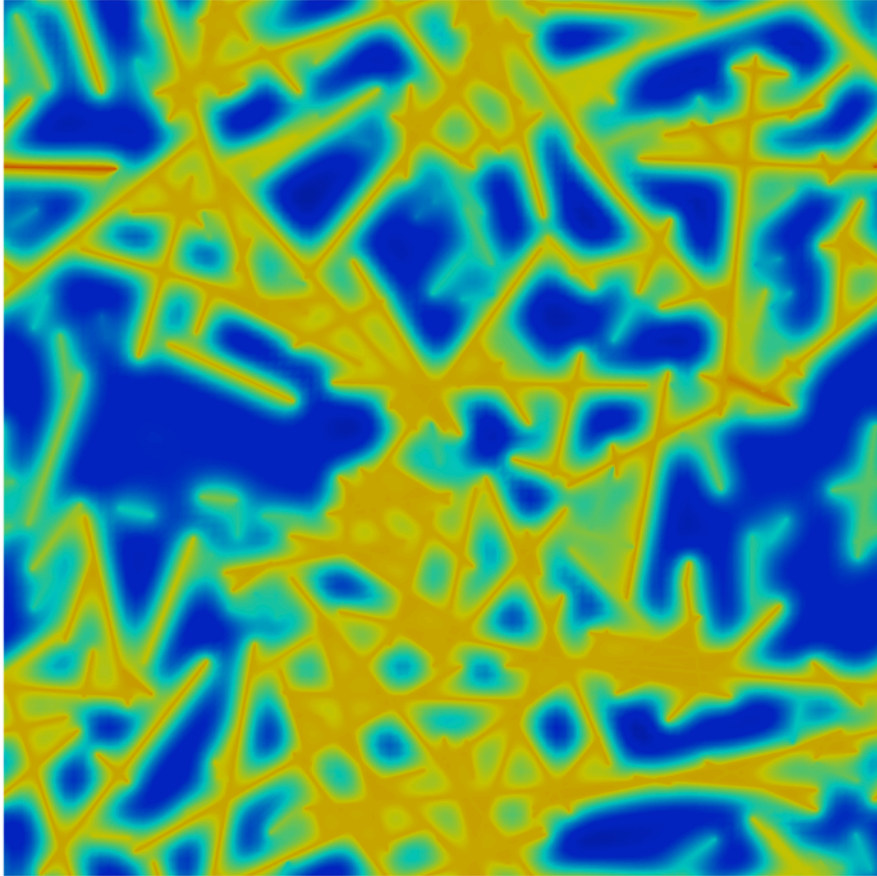
## Constant aperture

## Variable aperture

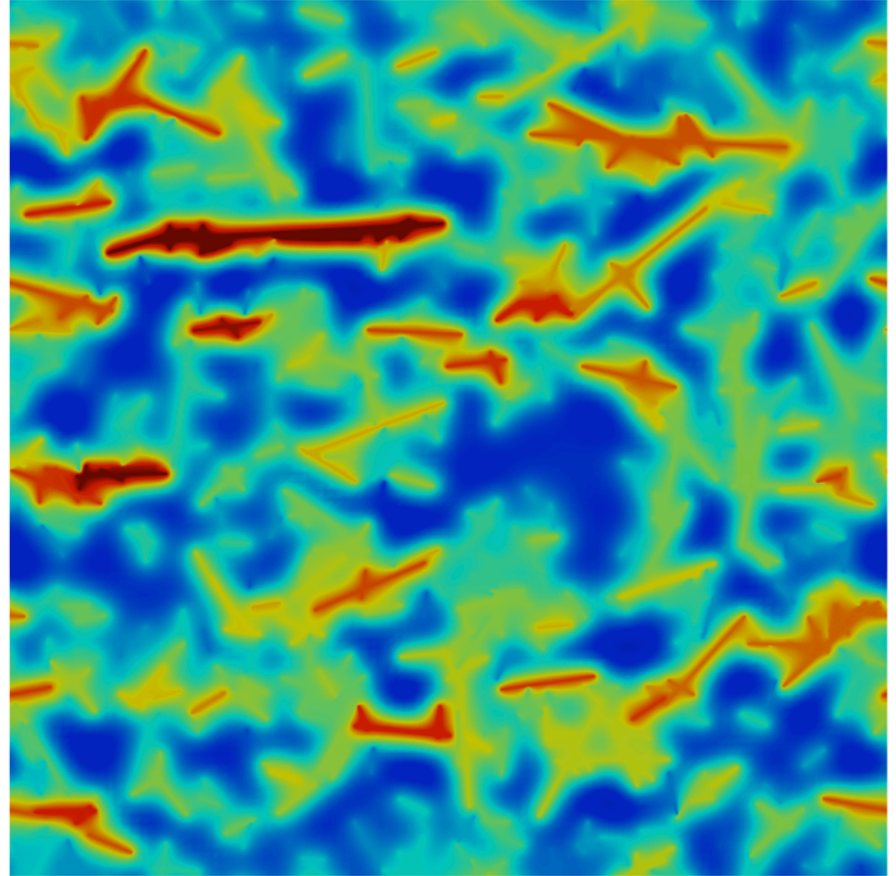


# Pressure fields

$a = 1.5$



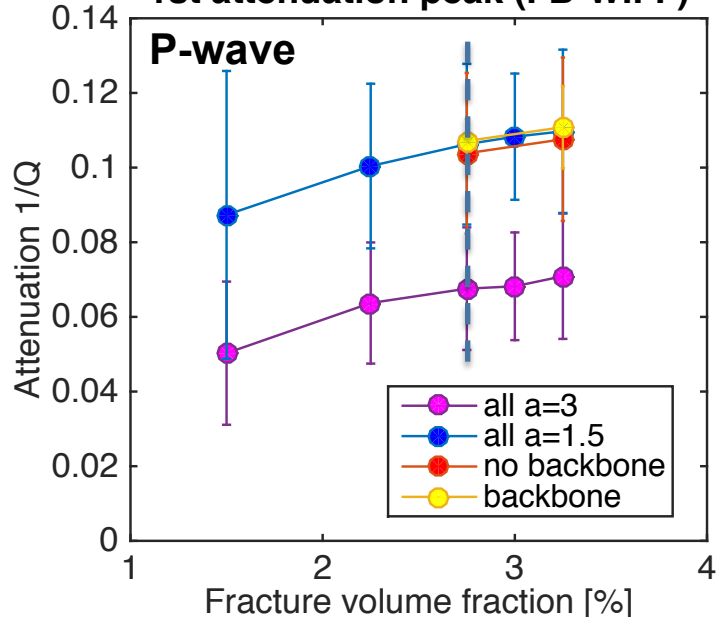
$a = 3$



# Attenuation trends: length distribution and fracture volume

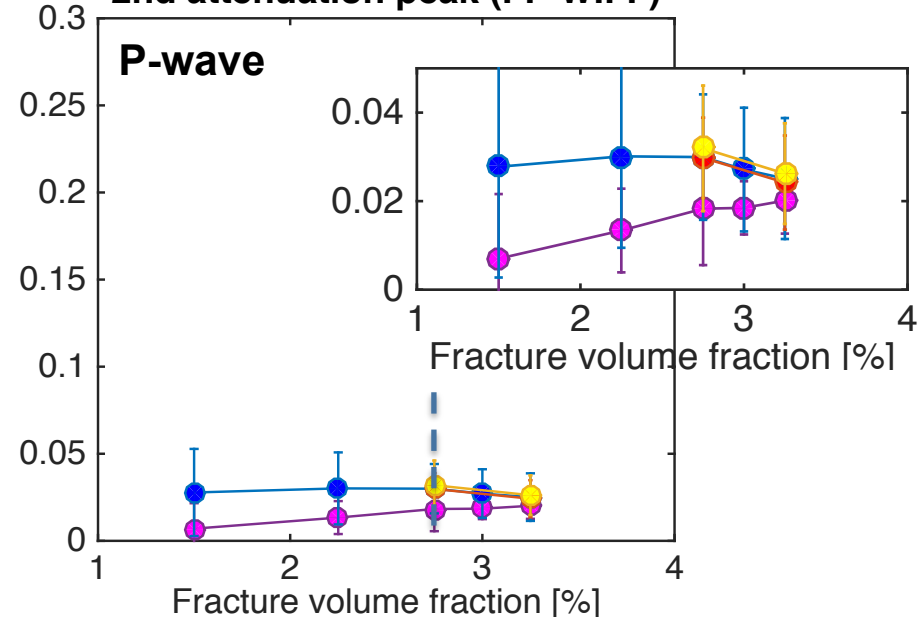
## 1st attenuation peak (FB-WIFF)

**P-wave**

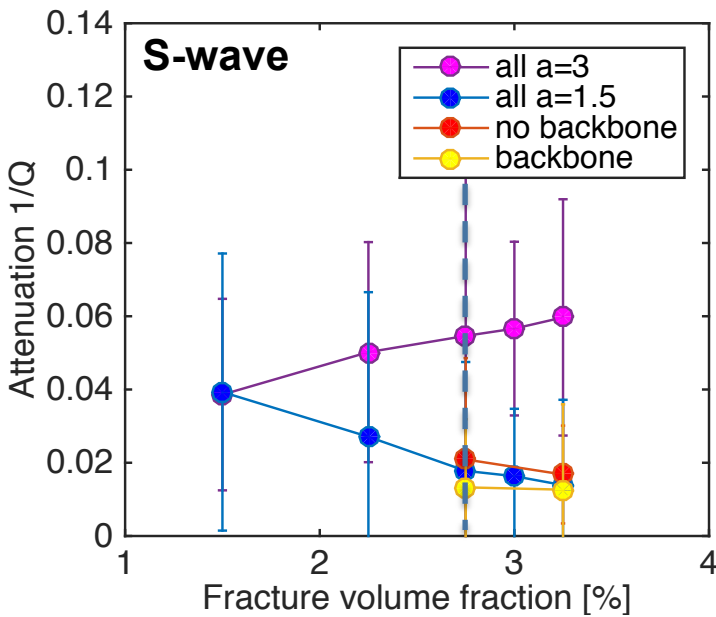


## 2nd attenuation peak (FF-WIFF)

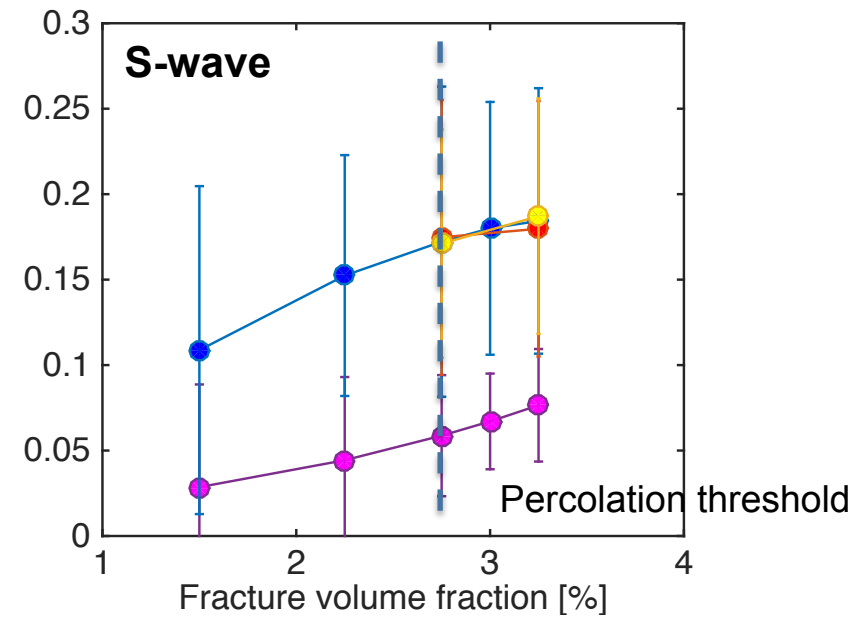
**P-wave**



**S-wave**

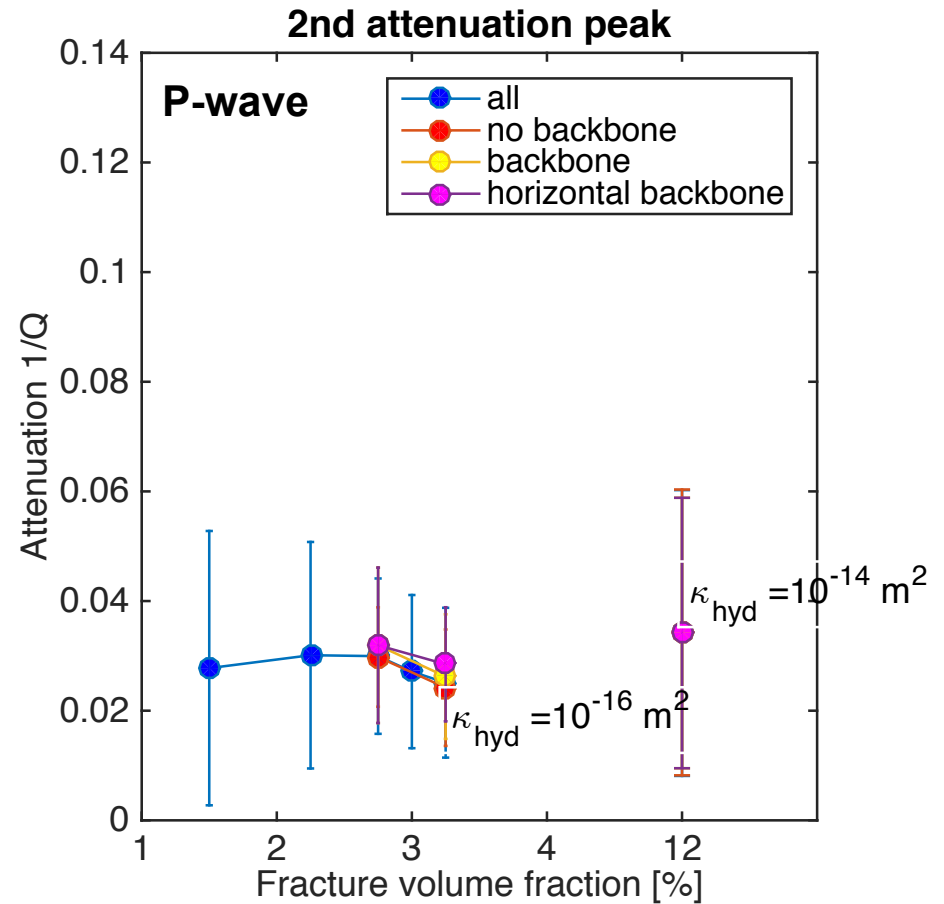
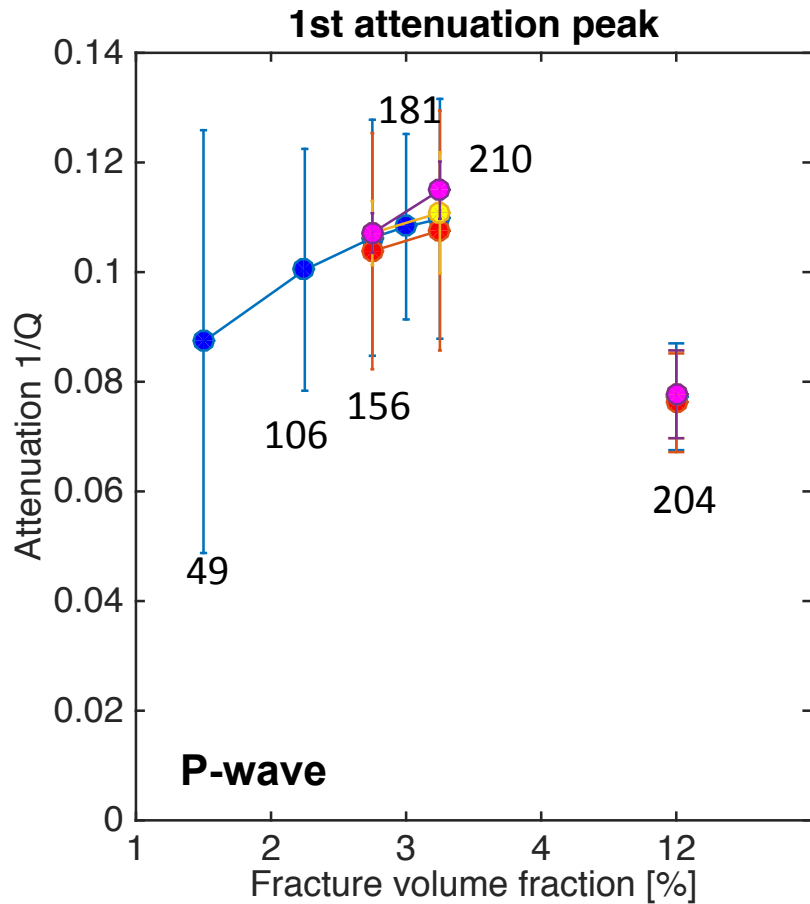


**S-wave**





# Comparison constant vs. variable aperture: Attenuation trends vs. fracture volume



**Fracture-to-fracture flow:** Increase with fluid storage volume within fractures (larger apertures!) but not necessarily number of connections!

# Conclusions

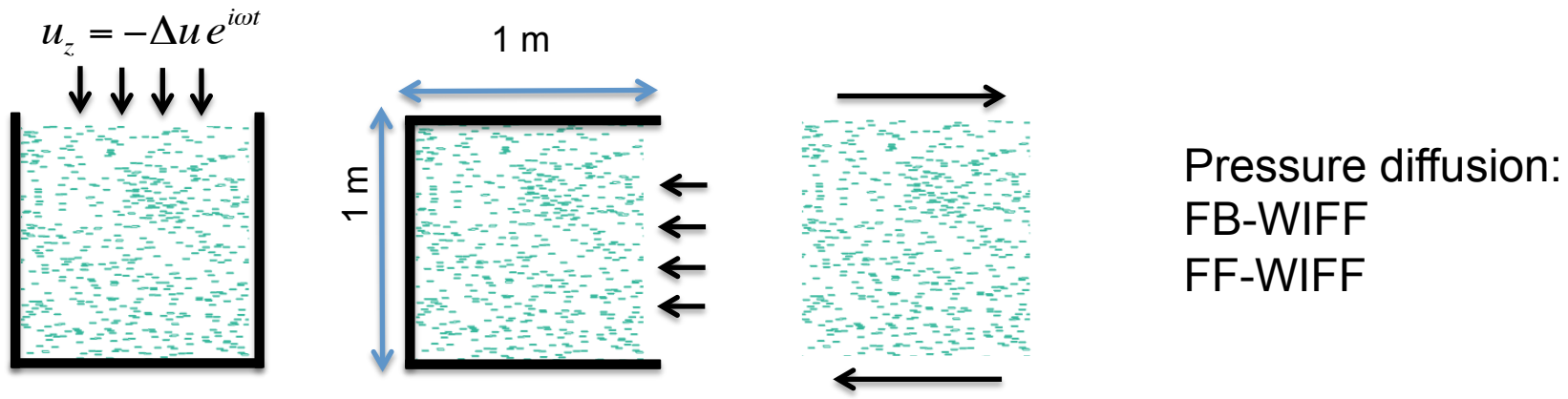
→ Establishing a direct relation between hydraulic conductivity and attenuation remains difficult !

## Seismic attenuation depends on:

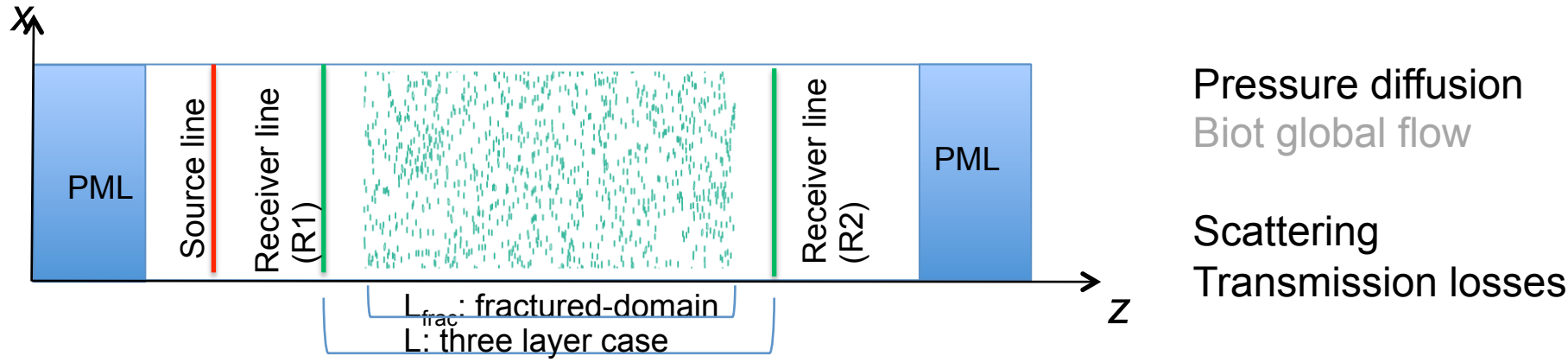
- Number of local connections
  - Size of fracture cluster
  - Fluid storage volume
  - Elastic interaction between fractures
  - Fracture length distribution
  - Orientation of fractures (isotropic networks)
- P-wave attenuation trends change close to percolation threshold
- Sensitive to the degree of local fracture network connectivity but not to the existence of a backbone !
- Differing P- and S-wave attenuation trends are a possible indicator of fracture connectivity

# Wave propagation effects: Oscillatory test vs transmission experiment

## Numerical upscaling based on Biot's quasi-static equations (QS)

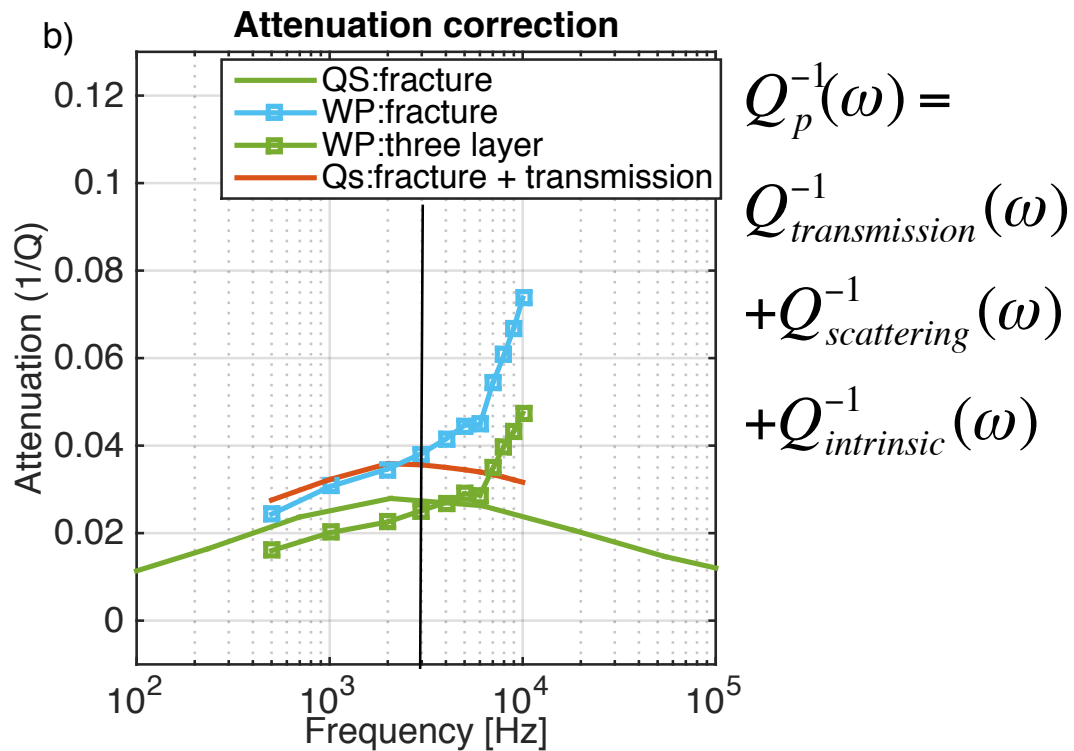
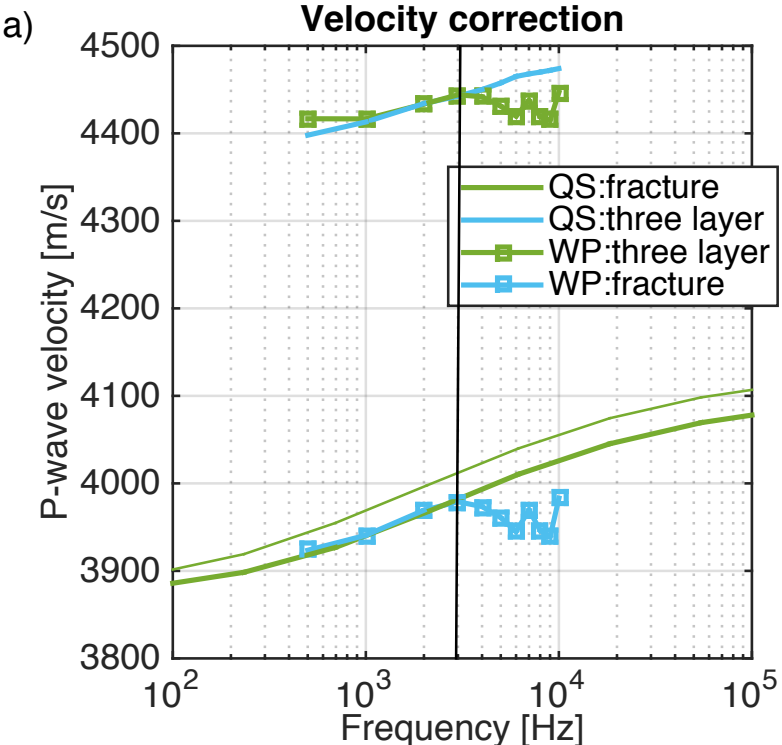
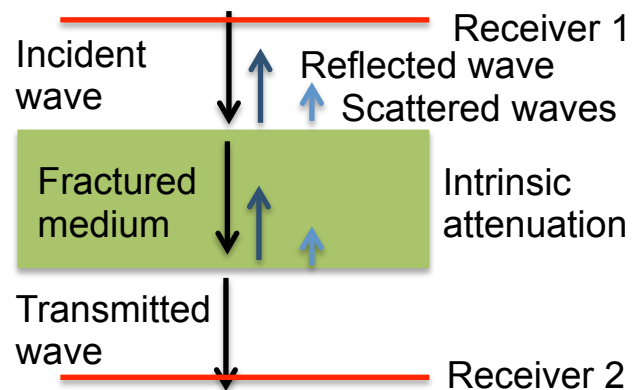
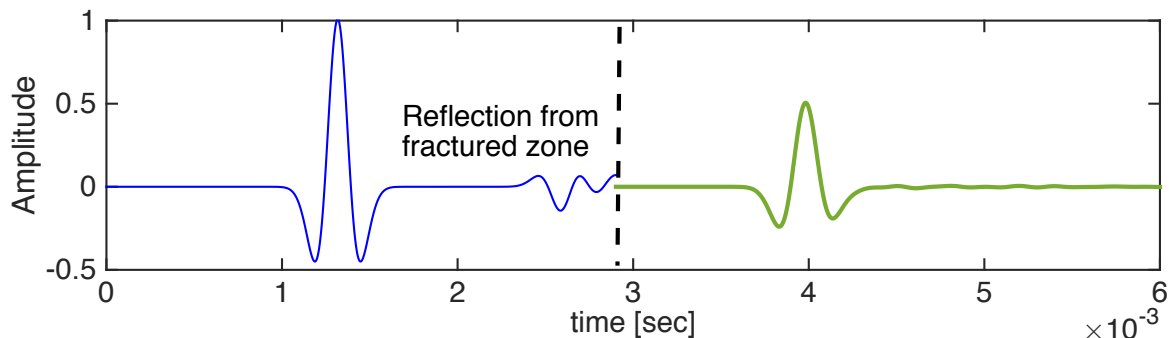


## Wave propagation modelling based on Biot's dynamic equations (WP)

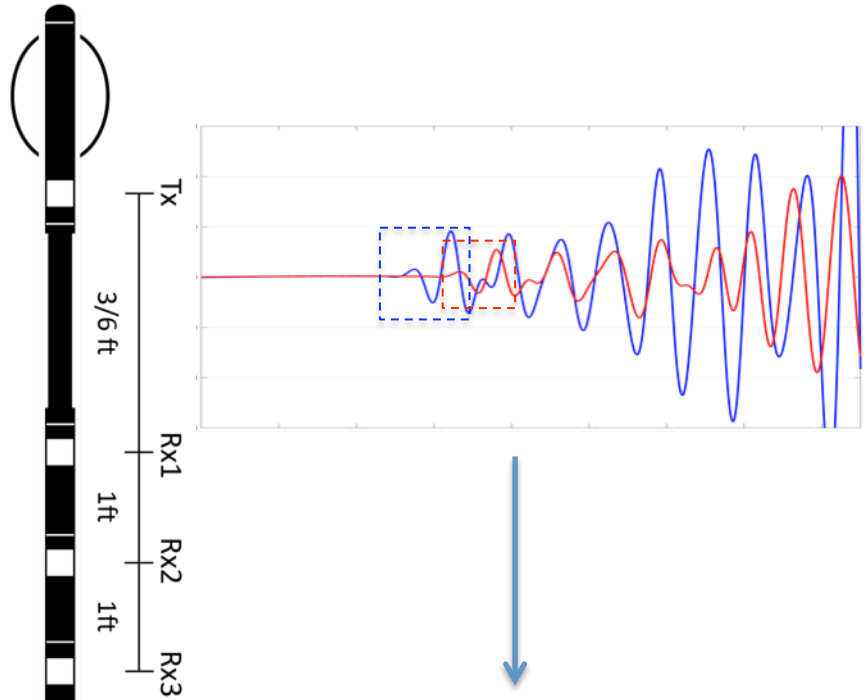


Domain size: 2 - 5 wavelengths (20 correlation lengths of the medium)

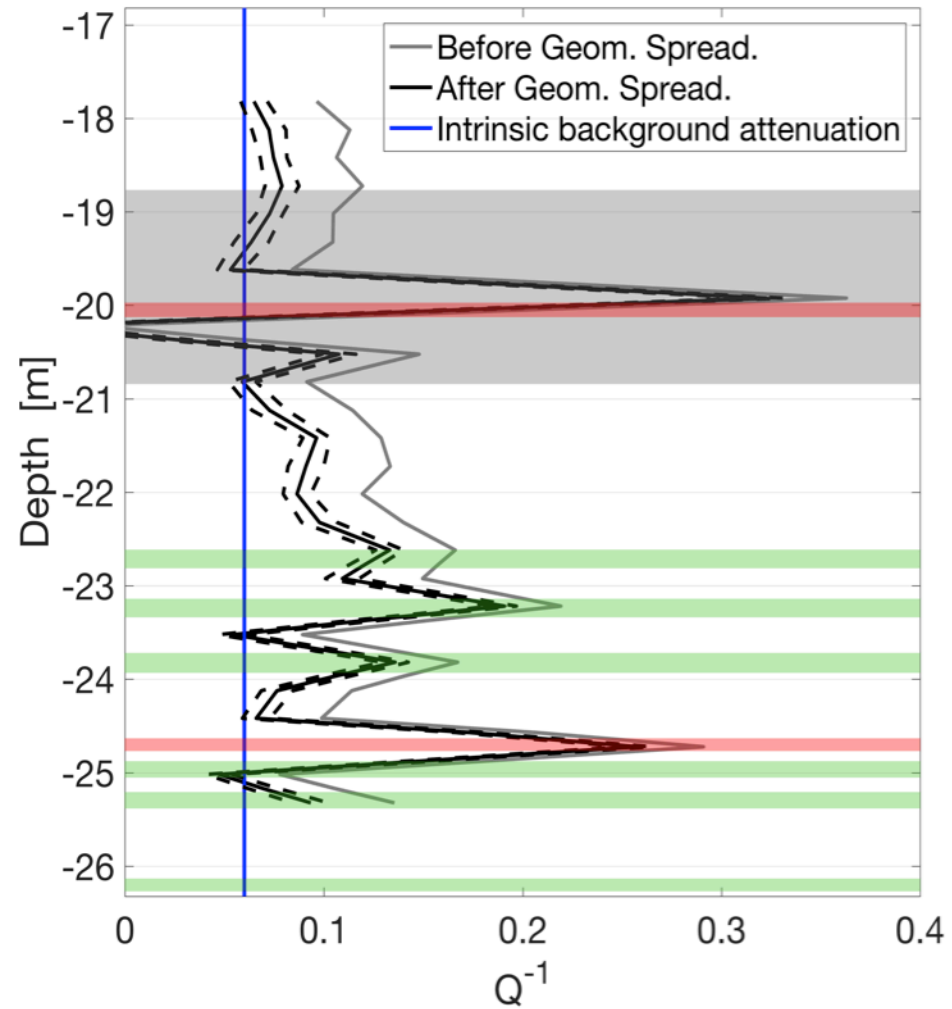
# Attenuation and velocity estimation



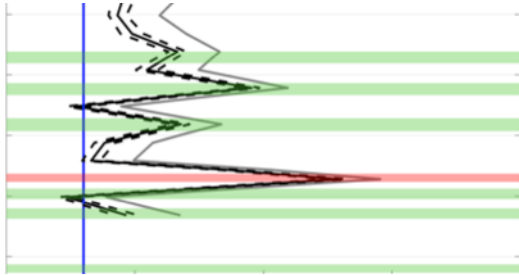
# Full-waveform sonic log measurements – Grimsel Felslabor (INJ2)



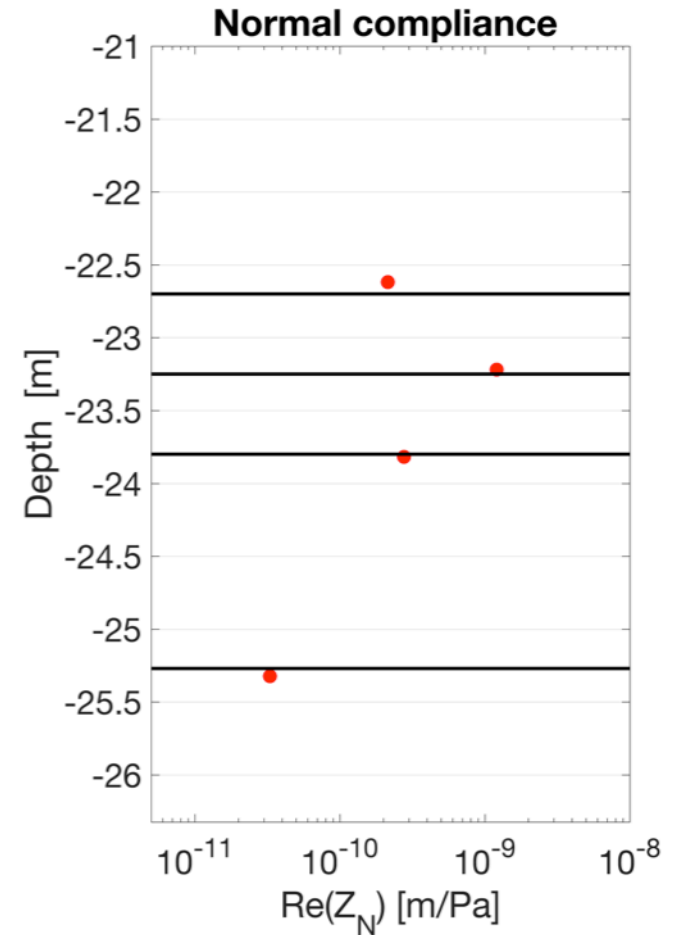
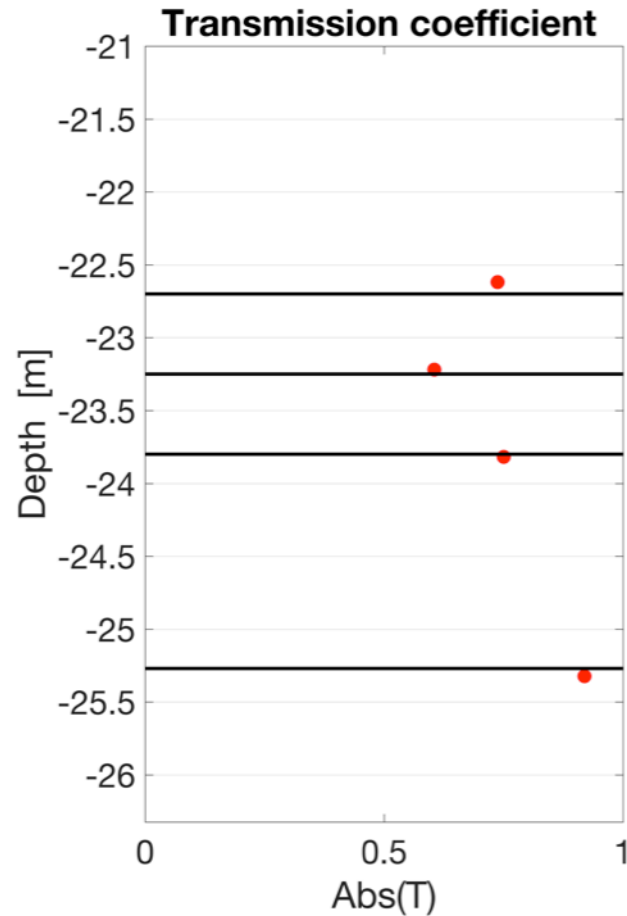
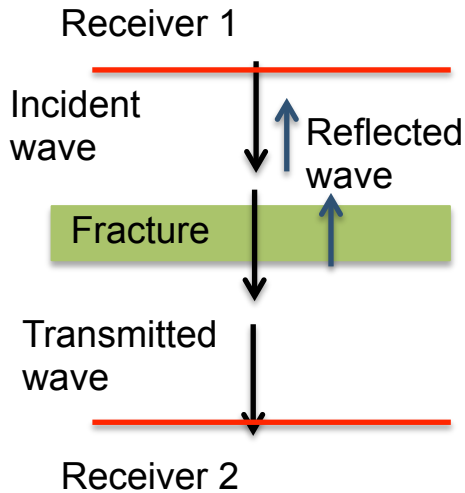
$$Q_p^{-1}(\omega) = Q_{spreading}^{-1}(\omega) + Q_{intrinsic}^{-1}(\omega) + Q_{transmission}^{-1}(\omega)$$



# Transmission coefficients and fracture compliance



+ Velocities  $\rightarrow$  Transmission coefficient  $\dashrightarrow$  Fracture compliance



# Poster

**Seismic attenuation in porous rocks containing stochastic fracture networks:** Jürg Hunziker, Marco Favino, Eva Caspari, Beatriz Quintal, J. Germán Rubino, Rolf Krause and Klaus Holliger

**Attenuation in fluid-saturated fractured porous media – quasi-static numerical upscaling vs dynamic wave propagation modeling:** Eva Caspari, Mikhail Novikov, Vadim Lisitsa, Nicolás D. Barbosa, Beatriz Quintal, J. Germán Rubino and Klaus Holliger

**Seismic transmissivity of fractures from full-waveform sonic log measurements:** Nicolás D. Barbosa, Eva Caspari, J. Germán Rubino, Tobias Zahner, Andrew Greenwood, Ludovic Baron, Klaus Holliger

**Efficient Finite Element Simulation Methods for Fracture Networks:** Marco Favino, Jürg Hunziker, Klaus Holliger, Rolf Krause

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**Towards fracture characterization using tube waves:** Jürg Hunziker, Shohei Minato, Eva Caspari, Andrew Greenwood and Klaus Holliger

**Characterization and imaging of a fractured crystalline hydrothermal fault zone from hydrophone VSP data:** A. Greenwood, E. Caspari, J. Hunziker, L. Baron, and K. Holliger.

**Geophysical characterization of a hydrothermally active fault zone in crystalline rocks – GDP 1 borehole, Grimsel Pass:** Eva Caspari, Ludovic Baron, Tobias Zahner, Andrew Greenwood, Enea Toschini, Daniel Egli and Klaus Holliger

**A numerical approach for studying attenuation in interconnected fractures:** Beatriz Quintal, Eva Caspari, Klaus Holliger and Holger Steeb

# Acknowledgements

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# Numerical upscaling

Biot's (1941) quasi-static poroelastic equations:

$$\nabla \cdot \boldsymbol{\sigma} = 0,$$

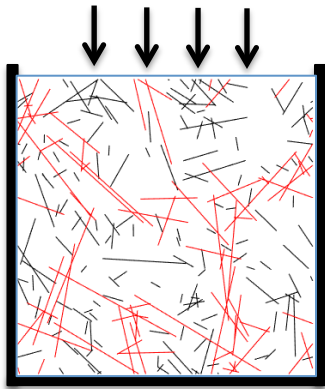
$$i\omega \frac{\eta}{k} \mathbf{w} = -\nabla p$$

$$\boldsymbol{\sigma} = \left[ (H - 2G) \nabla \cdot \mathbf{u} + \alpha M \nabla \cdot \mathbf{w} \right] \mathbf{I} + G \left[ \nabla \mathbf{u} + (\nabla \mathbf{u})^T \right],$$

$$-p = \alpha M \nabla \cdot \mathbf{u} + M \nabla \cdot \mathbf{w}$$

Compression test:

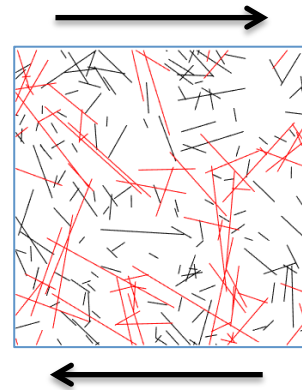
$$u_z = -\Delta u e^{i\omega t}$$



$$H(\omega) = \frac{\langle \sigma_{zz}(\omega) \rangle}{\langle \varepsilon_{zz}(\omega) \rangle}$$

$$Q_p^{-1}(\omega) = \frac{\Im(H(\omega))}{\Re(H(\omega))}$$

Simple shear test:



$$G(\omega) = \frac{\langle \sigma_{xz}(\omega) \rangle}{\langle 2\varepsilon_{xz}(\omega) \rangle}$$

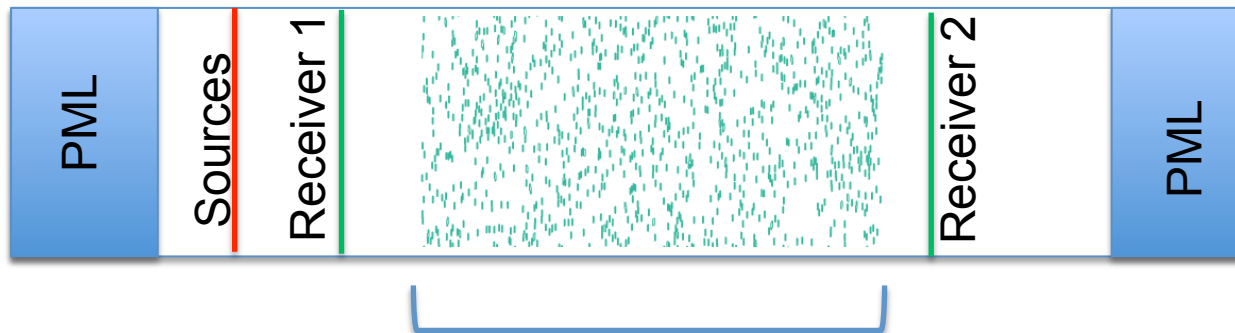
$$Q_s^{-1}(\omega) = \frac{\Im(G(\omega))}{\Re(G(\omega))}$$

## 2D Wave propagation transmission experiment (time domain)

Biot's (1962) **dynamic** poroelastic equations (after Masson and Pride, 2010)

$$\begin{aligned} \nabla \cdot \boldsymbol{\sigma} &= \rho \frac{\partial \mathbf{v}}{\partial t} + \rho_f \frac{\partial \mathbf{q}}{\partial t} \\ \rho_f \frac{T}{\phi} \frac{\partial \mathbf{q}}{\partial t} + \rho_f \frac{\partial \mathbf{v}}{\partial t} + \frac{\eta}{k_0} \mathbf{q} &= -\nabla p \end{aligned} \quad \left| \quad \begin{aligned} -\frac{\partial p}{\partial t} &= M (\alpha \nabla \cdot \mathbf{v} + \nabla \cdot \mathbf{q}) + \mathbf{s}_f, \\ \frac{\partial \boldsymbol{\sigma}}{\partial t} &= (\lambda_u \nabla \cdot \mathbf{v} + \alpha M \nabla \cdot \mathbf{q}) \mathbf{I} + \mu [\nabla \mathbf{v} + (\nabla \mathbf{v})^T] + \mathbf{s}. \end{aligned}$$

Wave propagation transmission experiment:



$\frac{\eta}{k_0}$  Steady limit of permeability:  
Neglects viscous boundary layers!

Domain size: 2 - 5 wavelengths (20 correlation lengths of the medium)

Attenuation: spectral-ratio type method

# Fractured medium

**Background:** stiff porous matrix of low porosity and permeability

**Fractures:** compliant inclusion of high porosity and permeability

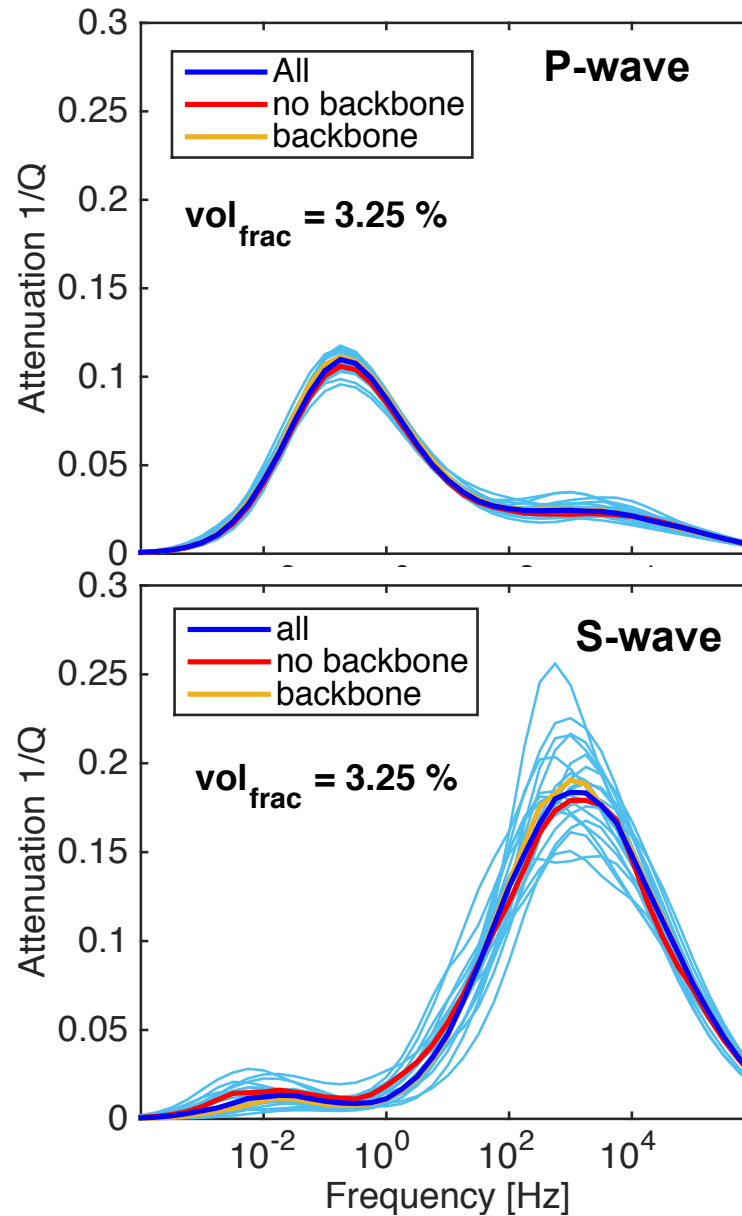
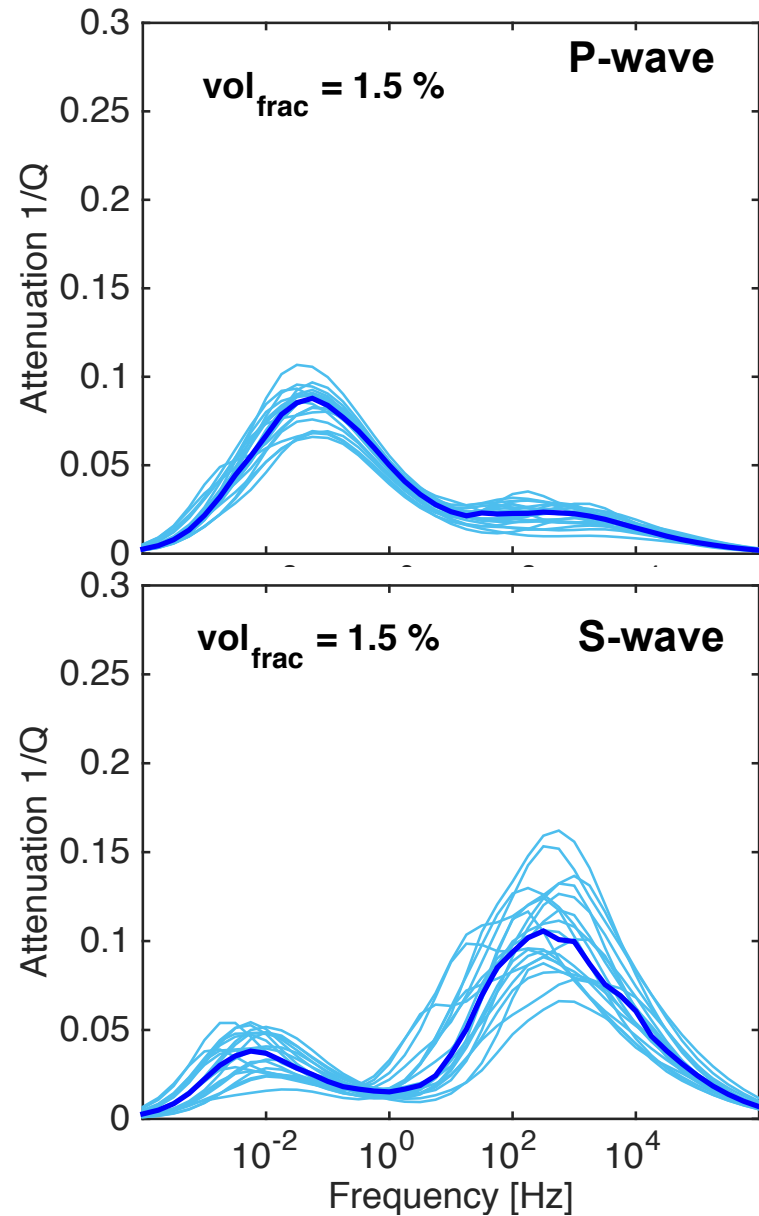
	Background	Fracture	Fluid
Bulk modulus [Gpa]	34	0.025	2.4
Shear modulus [GPa]	32	0.02	
Porosity	0.06	0.5	
Permeability [m <sup>2</sup> ]	10 <sup>-18</sup>	10 <sup>-11</sup> (0.5 10 <sup>-11</sup> - 10 <sup>-10</sup> )	

**Fracture network parameter:** Power law length distribution

$$n(l, L) = d_{frac} (a - 1) \frac{l^{-a}}{l_{min}^{-a+1}} \text{ for } l \in [l_{min}, l_{max}]$$

	Constant	Variable
Exponent a	1.5	1.5
Length $l_{min}, l_{max}$ [mm]	10, 200	10, 200
Fracture volume $d_{frac}$ [%]	1.5 – 3.25	12
Aperture [mm]	0.5	0.7 - 3

# Constant aperture: P- and S-wave attenuation



Fracture-to-background flow is dominant for P-waves

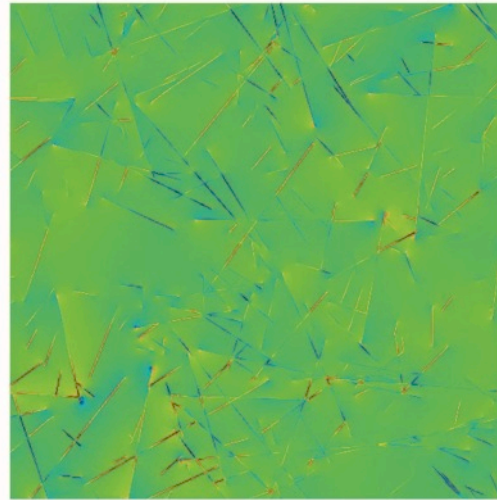
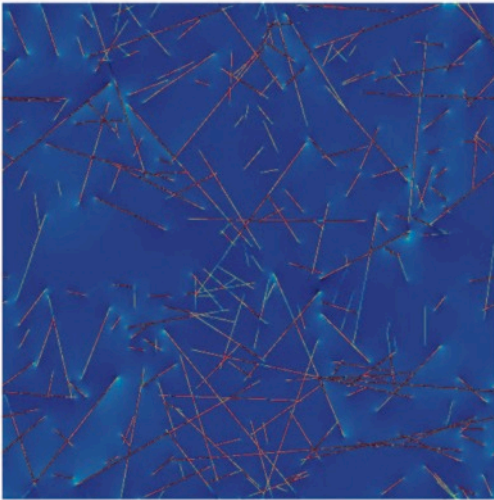
Fracture-to-fracture flow is dominant for S-waves

# Pressure fields

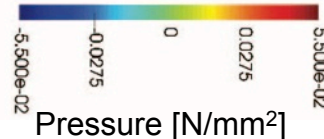
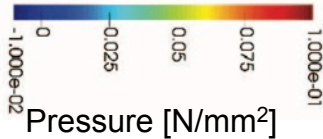
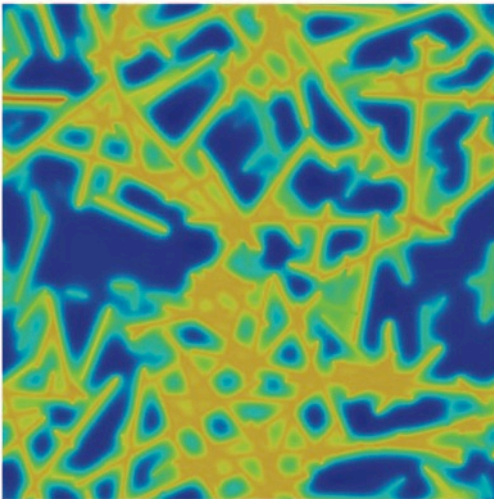
P-wave

S-wave

Highest frequency



Low frequency peak



Fracture-to-fracture flow is dominant for S-waves

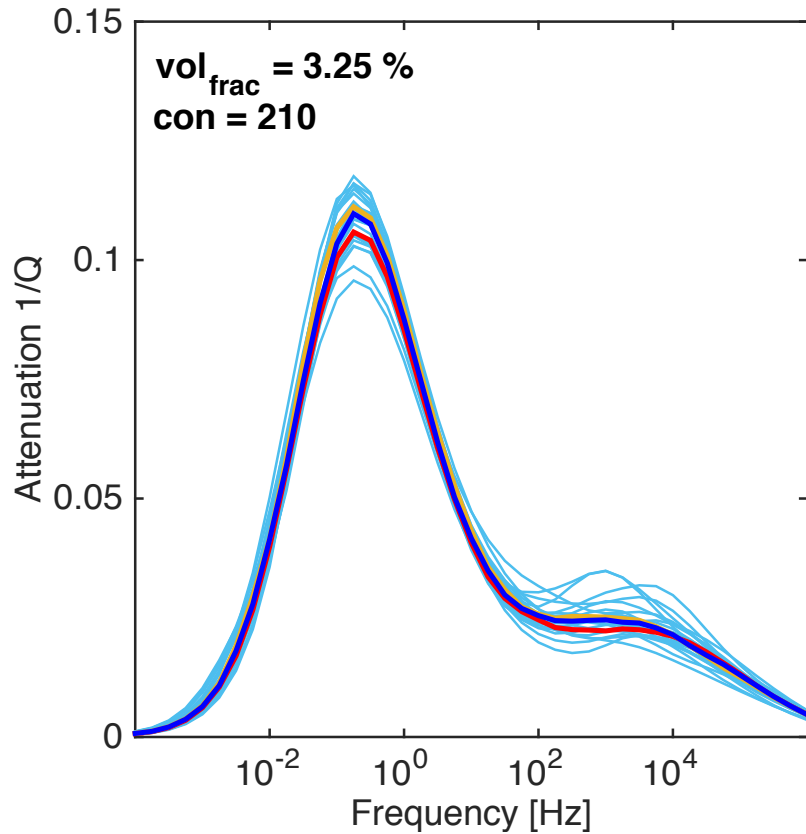
→ Larger induced pressure gradients

Fracture-to-background flow is dominant for P-waves

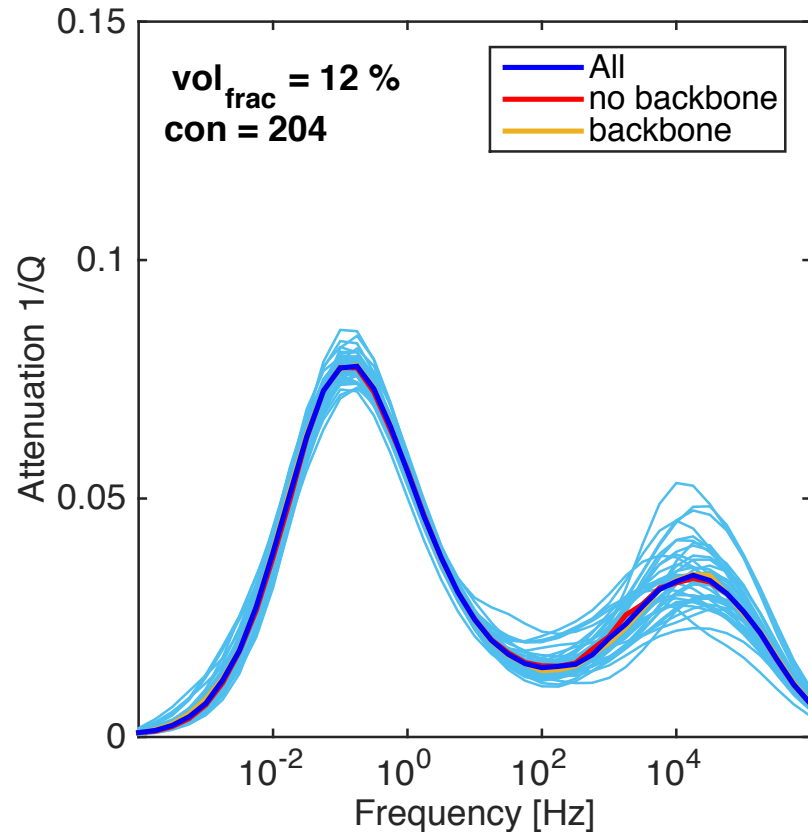
→ Larger remaining pressure gradients

# Comparison constant vs. variable aperture: P-wave attenuation

Constant aperture



Variable aperture



- Same degree of connectivity
- Increase in fluid storage volume within fractures (larger apertures!)